# SPROUT - Smart Power ROUting Tool for Board-Level Exploration and Prototyping

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*Abstract*—The board-level power network design process is governed by system-level parameters such as the number of layers and the ball grid array (BGA) pattern. These parameters influence the characteristics of the resulting system, such as power, speed, and cost. Evaluating the impact of these parameters is, however, challenging. To estimate the reduction in impedance if, for example, additional BGA balls are dedicated to the power delivery system, adjustments to the board layout and an additional impedance extraction process are required. These processes are poorly automated, requiring significant time and labor. Automating power network exploration and prototyping can greatly enhance the board-level power delivery design process by increasing the number of possible design options. With power network exploration and prototyping, the effects of the system parameters on the electrical characteristics can be better understood, providing valuable insight into early stages of the design process. SPROUT – an automated algorithm for prototyping printed circuit board (PCB) power networks – is presented here. This tool includes the first fully automated algorithm for boardlevel power network layout synthesis. Two board-level industrial power networks are synthesized using SPROUT. The impedance of the resulting layouts exhibits good agreement with manual PCB layouts while significantly reducing the design time. The tool is used to explore area/impedance tradeoffs in a three rail system, providing useful data to enhance the PCB design process.

#### I. INTRODUCTION

Modern high performance VLSI systems require stable power [1]. Voltage scaling combined with shrinking interconnect dimensions and increasing current consumption result in significant power noise, degrading power integrity [2]. Fast transition times significantly broaden the spectrum of the power noise. Different strategies are employed at the die, package, and board levels to mitigate this power noise. The board-level power delivery network is a crucial component of the power delivery system, connecting the power management integrated circuit (PMIC) with the die or package. Careful design of the board level power delivery system is crucial for connecting the power management IC with the package or die as well as the on-board decoupling capacitors.

The flow of the power delivery design process for printed circuit boards (PCB) is illustrated in Fig. 1. The quality and



Fig. 1. Conventional design flow for power delivery networks for printed circuit boards.

cost of the PCB is governed by a set of system-level parameters, such as the location and model of the components, and the number and thickness of the metal layers. These parameters affect the floorplan and placement of the components. After the location of the components is known, the power management IC is connected to the target ball grid array and decoupling capacitors. If the impedance profile of the resulting layout does not satisfy the target requirements, the layout is iteratively adjusted. These adjustments range from minor changes to the routed shape to altering the entire floorplan. Several iterations are often necessary to comply with the target impedance requirements [3].

The influence of the system parameters on power integrity and cost is qualitatively well understood. For example, adding decoupling capacitors would likely reduce the inductive noise while adding cost. Quantifying these effects prior to floorplanning and routing is however difficult. Due to the lack of information at early stages of the system design process, the system level parameters are often arbitrarily chosen. These power delivery systems may fail to satisfy target impedance requirements, leading to a costly redesign process. Early exploration of the design space may eliminate or decrease the number of layout adjustments at later stages of the design process.

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Fig. 2. Proposed prototyping flow for printed circuit boards using SPROUT. The PCB layout parameters are the inputs to SPROUT that produce a prototype of the power network. The parasitic impedance of the prototype is estimated. This process is repeated for different sets of system-level parameters. The power, performance, and cost of each prototype is evaluated and compared to other prototypes to determine the most favorable system parameters.

The objective of the proposed Smart Power ROUTing algorithm for printed circuit boards (SPROUT) is to produce a prototype of the power network based on a target set of design parameters (see Fig. 2). The resulting layout is suitable for impedance extraction. Therefore, the impedance of the layout based on the target set of design parameters may be efficiently and automatically evaluated. This capability supports a more rigorous evaluation of the design space and better exploration of design tradeoffs, such as cost and performance. An informed choice of design parameters early in the development process reduces the likelihood of not satisfying the target impedance. In addition, the layout prototype may guide the final layout, further accelerating the development process.

On-chip signal routing is a well established subject in the research community [4], [5], [6], [7], [8]. Signal routing is however significantly different from the problem discussed in this paper as described in table I. The number of on-chip signal terminals exceeds thousands, whereas fewer than 20 voltage domains are supported by a board level power network. On-chip signal nets are typically routed via rectilinear metal tracks, whereas board-level power shapes can have an arbitrary form. Design priorities and constraints for signal and power routing are also different. Characteristics prioritized in signal

routing include crosstalk, attenuation, impedance matching, inter-symbol interference, timing, and mode conversion. Different metrics are prioritized in power routing, such as current density, thermal profile, and resistive and inductive noise.

Unlike automated signal routing, which is extensively studied in the literature, the automated *synthesis* of board-level power nets has received minimal attention. Most works in the literature focus on the analysis of existing power delivery networks. For example, in [9], [10], [11], [12], fast methods for estimating the impedance of board-level power networks are described. In [13], a simplified circuit model is presented to evaluate inductive power noise. An accurate PCB analysis methodology is proposed in [14] where the finite difference model is integrated with SPICE. Methods for enhancing electromagnetic compatibility and power integrity are discussed in [4], [5], [6], [7], [8]. IC power network synthesis has been discussed in the literature. Decoupling capacitor selection and placement is a common topic [4], [15], [16]. In [17], the top layers of an IC power network with minimal congestion are synthesized. Using a neural network, a nonuniform power mesh that minimizes routing congestion is generated while satisfying electromigration and voltage drop constraints.

Several features distinguish on-chip and board-level power network synthesis. The top layers of the IC power network are often structured as a mesh [1], [18], [19]. The current is supplied to the load using vias and orthogonal wires. The PCB power network does not typically span the entire layout. Instead, specific areas of the PCB, namely, the PMIC output, ball grid array (BGA), and, optionally, decoupling capacitors, are connected using an arbitrarily shaped metal segment.

SPROUT is the first automated power network prototyping tool for PCBs, initially presented in [20]. Major contributions of this paper include application of graph-based optimization to the synthesis of board-level power network layout, and a multilayer power network routing algorithm. The remaining portion of this paper is organized as follows. In section II, the power routing algorithm is described. The algorithm is validated using industrial case studies in section III. Some conclusions are provided in section IV. A modification of SPROUT to support multilayer routing is described in the Appendix.

## II. SPROUT ALGORITHM

A typical board-level layout consists of several metal layers, each separated by a dielectric layer. The connections between the layers are provided by vias. SPROUT uses layer information, design rules, and placement data to produce an initial layout. The objective of the algorithm is to generate a shape connecting the power management IC with the target ball grid array (BGA) balls and decoupling capacitors while complying

TABLE I COMPARISON BETWEEN SIGNAL AND BOARD-LEVEL POWER ROUTING

<b>Feature</b>	<b>Signal Routing</b>	<b>Board-level Power Routing</b>
Goal	Connect signal source and destination locations	Connect power management IC with ball grid array
Resulting geometry	Rectilinear metal tracks	Arbitrary shaped metal segment
Typical number of nets	More than 50	Less than ten
Typical constraints	Crosstalk noise, timing	Current density, temperature, metal resources



Fig. 3. Overview of SPROUT algorithm. The available space  $A_n$  is converted into an equivalent graph  $\Gamma_n$ . The subgraph seed  $\Gamma_n^s$  is generated by SPROUT and expanded using the SmartGrow algorithm described in section II-D. After achieving the target area, the nodes in  $\Gamma_n^s$  are rearranged using the SmartRefine algorithm to enhance the electrical characteristics. The final subgraph is converted into a physical layout.

with the design rules and minimizing the impedance between the terminals. Note that the resulting prototype is not the final topology but a prototype used to estimate the effects of the design parameters on system performance.

Similar to many signal routing algorithms, SPROUT works in the graph domain, permitting the exploitation of powerful graph-based algorithms. An overview of the proposed algorithm is shown in Fig. 3. The space available for routing is initially determined from the input layout, as described in subsection II-A. This layout is converted into a graph, and the initial seed connection is established between the terminals as described in, respectively, subsections II-B and II-C. SmartGrow and SmartRefine algorithms are introduced in, respectively, subsections II-D and II-E. Using these algorithms, the impedance between the terminals is iteratively reduced by adding and rearranging the nodes. A subgraph reheating technique, inspired by simulated annealing, is proposed in subsection II-F where the size of the graph is temporarily increased to reduce the probability of a suboptimal impedance. In subsection II-G, the placement of the resulting graph into the original layout is desc2ribed. The complexity of SPROUT is discussed in subsection II-H.

#### *A. Available routing space*

An assessment of the available space commences with processing the input information. Each element of the layout is converted into a polygon with four parameters, layer, net, geometry, and buffer. To understand each component, consider three vias placed on the top layer of a PCB (see Fig. 4a). The via pads are converted into polygons. Assuming the vias are placed on layer 1, the layer parameter of the corresponding polygons is 1. Each capacitor pad is assigned a net, namely  $V_{DD}$  and  $V_{SS}$ . The geometry of each pad is expressed as an ordered set of coordinates. To decrease the likelihood or minimize the effects of manufacturing defects such as unintended shorts, spurs, underetches, and electromagnetic interference [21], each geometry is assigned a buffer. This buffer ensures polygons from different nets are properly spaced. To illustrate the buffering process, consider the example shown in Figs. 4b and 4c. Contact between the two  $V_{DD}$  vias is not possible using a straight interconnect segment because this segment intersects the buffer of the  $V_{SS}$  via, and the via intersects the buffer of the interconnect. The bent interconnect segment shown in Fig. 4c produces a valid connection since the geometries do not intersect the buffers of the other nets.



Fig. 4. One  $V_{SS}$  (vertical hatch), two  $V_{DD}$  (horizontal hatch) via pads (dark), and buffers (light). a) Initial layout. b) The connection to the  $V_{DD}$  vias is invalid since the buffer around the  $V_{DD}$  connection overlaps the  $V_{SS}$  via, and the  $V_{DD}$  connection overlaps the  $V_{SS}$  via buffer. c) Example of valid routing. Neither the  $V_{DD}$  nor the  $V_{SS}$  buffer intersects the vias or connections to a different net. Note that the  $V_{DD}$  connection can be placed in the buffer around the  $V_{DD}$  vias because both the via and connection belong to the same net.



Fig. 5. Available space (shaded) for  $V_1$  in two layouts. a) Layout (left) where routing from the pad on the left to four vias is possible, as evident from the connected available space (right). b) Layout (left) where connecting a pad with a via is not possible within a single layer due to the disjoint available space (right).

Note that it is legal for a  $V_{DD}$  polygon to cross a  $V_{DD}$  buffer because these polygons belong to the same net.

The entire design space  $U$  is initially viewed as available for routing. The available space  $A_n$  for a particular net n is determined by removing buffers of the other nets from the design space.

$$
A_n = U \setminus \bigcup_{n_j \neq n} b_j.
$$
 (1)

Polygon removal is achieved by utilizing efficient polygon clipping algorithms [22], [23] that require negligible time, as discussed in subsection II-H. After removal, the available space on each layer may become disjoint, leaving no valid path between terminals on the same layer, as illustrated in Fig. 5. In this case, routing is accomplished using multiple layers. Based on the algorithm described in the Appendix, the multilayer routing problem is decomposed into several single layer routing problems.





Fig. 6. Conversion of irregularly shaped tiles into an equivalent graph. a) Tiles A and B have a twice wider contact than tiles B and C, and b) nodes A and B have double conductance as compared to nodes B and C.

**Algorithm 1** Convert available space  $A_n$  into equivalent graph  $\Gamma_n$  using tiles of size  $(\Delta x, \Delta y)$ 

```
1: procedure SPACETOGRAPH(A_n, \Delta x, \Delta y)2: V_n \leftarrow \varnothing3: E_n \leftarrow \varnothing4: [x_{min}, x_{max}, y_{min}, y_{max}] \leftarrow bounds(A_n)5: n_x \leftarrow \left\lfloor \frac{x_{max} - x_{min}}{\Delta x} \right\rfloor6: n_y \leftarrow \begin{bmatrix} \frac{y_{max}-y_{min}}{\Delta y} \end{bmatrix}7: for i = 0, 1, 2, \ldots, n_x8: x_{min}^i \leftarrow x + i\Delta x, x_{max}^i \leftarrow x + (i+1)\Delta x9: for j = 0, 1, 2, ..., n_y10:y_{min}^j \leftarrow y + j\Delta y, y_{max}^j \leftarrow y + (j+1)\Delta y11: box_{i,j} \leftarrow rectangle(\lbrace x_{min}^i, y_{min}^j \rbrace, \lbrace x_{max}^i, y_{max}^j \rbrace)12: cell_{i,j} \leftarrow box_{i,j} \cap A_n13: if cell_{i,j} \neq \emptyset14: Add cell_{i,j} to V_n15: overlap_y = cell_{i,j} \cap cell_{i,j-1}16: if overlap<sub>y</sub> \neq \emptyset17: Add \{cell_{i,j}, cell_{i,j-1}, \frac{length(overlap_y)}{\Delta x}\} to E_n18: overlap_x = cell_{i,j} \cap cell_{i-1,j}19: if cell_{i,j} \cap cell_{i-1,j} \neq \emptyset20: Add {cell_{i,j}, cell_{i-1,j}, \frac{length(overlap_x)}{\Delta y}} to E_n21: return \Gamma_n = (V_n, E_n)
```
#### *B. Equivalent graph*

Once the available space of the layout is determined, it is converted into an equivalent graph  $\Gamma_n$ , as described in Algorithm 1. The available space  $A_n$  is divided into tiles  $a_n$ . Using a bijective map,

$$
f: A_n \leftrightarrow \Gamma_n,\tag{2}
$$

each tile  $a_n$  becomes a node  $\gamma_n$  within the graph. This mapping is recorded and used in the last stage of the algorithm to convert each node back into a tile. The dimensions  $\Delta_x$  and  $\Delta_{y}$  of the tiles are set in advance and affect the performance of the algorithm, as described in subsection II-H. Finer tiling produces smoother shapes and a smaller resistance at the cost of additional runtime. Due to the irregular shape of the available space, tiles near the boundaries may be irregular in shape, as shown in Fig. 7.

The adjacent vertices in the equivalent graph are connected with edges. To mimic the electrical behavior of the rail, the weight of the edges is proportional to the conductance between adjacent tiles. An accurate estimate of the resistance between arbitrary shapes requires computationally expensive methods, such as the finite element method [24]. For routing, however, a more efficient heuristic is proposed. The conductance of each



Fig. 7. Conversion of the available space for net  $V_2$  into an equivalent graph. a) The available space is split into unit cells. Cells with irregular shapes are shaded. b) Equivalent graph. The tiles overlapping vias are treated as a single node. Nodes are not generated in prohibited areas.



Fig. 8. Example of graph-based routing process among three terminals. a) Initial seed subgraph, b) voidless subgraph after filling the internal voids, c) initial stage of subgraph growth, and d) final stage of subgraph growth. Areas with large current are reinforced with new nodes. e) Initial stage of the refinement process. Areas with small current, specifically those nodes near the terminals, are replaced by nodes in the areas of current crowding, *i.e.*, closer to the obstacles. f) Final stage of the refinement process. The reduction in impedance is negligible, triggering termination of the algorithm.

edge is proportional to the width of the contact between two corresponding tiles. For example, the conductance between tiles A and B in Fig. 6 is twice larger than the conductance between tiles B and C due to the wider contact.

## *C. Seed subgraph*

Once the available space is converted into an equivalent graph  $\Gamma_n$ , the power routing problem is transformed into finding the subgraph  $\Gamma_n^s \in \Gamma_n$  connecting the terminal nodes such that the resistance between terminals is minimized. The order of the subgraph  $|V_n^s|$  is limited by the preset area constraint  $A_{max}$ . In SPROUT, the routing process commences with determining the initial connection between the source and target terminals. The location of the source and target terminals is supplied externally as a set  $T_n = \{t_n^1, \ldots, t_n^k\}$ . Efficient routing algorithms exist to determine the shortest path, such as Dijkstra [25] and Bellman-Ford [26]. This seed subgraph is iteratively improved using SmartGrow and SmartRefine algorithms, as described in, respectively, subsections II-D and II-E.

To generate the seed subgraph, the shortest path is determined for each pair of nodes, as shown in Fig. 8a. The resulting subgraph is directly passed to the SmartGrow algorithm. To accelerate convergence, however, the nodes located within the boundary of the seed are added to the subgraph, producing a subgraph without voids, as illustrated in Fig. 8b.

## *D. Growth stage*

The seed subgraph typically exhibits high resistance. The impedance of the subgraph can be improved by increasing the order  $|V_n^s|$  of the subgraph. To identify those parts of the subgraph that benefit most from reinforcement, a node current metric is introduced here. Those regions within the subgraph with the highest node current metric indicate a high current density. Additional nodes would likely produce a significant reduction in the impedance. In contrast, those regions with a smaller node current would produce a negligible reduction in impedance, resulting in suboptimal allocation of metal resources. These low current density regions are therefore left unchanged.

The node current metric is evaluated in three stages. The current is initially injected into each pair of terminals. The magnitude of the current is proportional to the expected current carried by the connection. For example, those pairs of terminals with large current, e.g., between the PMIC and the

**Algorithm 2** Generate voidless seed subgraph  $\Gamma_n^s = (V_n^s \in$  $V_n, E_n^s \in E_n$  such that terminals in set  $\Theta_n \in V_n$  are connected. 1: **procedure**  $\text{SEED}(\Gamma_n, \Theta_n = \{\theta_1, \ldots, \theta_k\})$ 

2: 
$$
V_n^s \leftarrow \varnothing
$$

- 3: for each node  $\theta_i$  in  $\Theta_n$
- 4:  $paths \leftarrow \text{SHORTESTPATH}(\Gamma_n, \theta_i, \{\theta_i + 1, \dots, \theta_k\})$
- 5: Add paths to  $V_n^s$  and  $E_n^s$
- 6:  $poly \leftarrow \text{EXTERIOR}(\bigcup(V_n^s))$
- 7: **for** each node v in  $V_n$
- 8: **if**  $v \cap poly \neq \emptyset$
- 9: Add v to  $V_n^s$
- 10: Add edges adjacent to v to  $E_n^s$

$$
\text{11:} \quad \textbf{return } \Gamma_n^s = (V_n^s, E_n^s)
$$

BGA balls, are injected with larger current as opposed to those pairs requiring relatively smaller current, such as connections between BGA balls. This current injection process is expressed as a current injection matrix,  $E \in R^{(|\Gamma_S| - 1) \times n_{pairs}}$ . Each column of  $E$  corresponds to a node within the subgraph. All entries in  $E$  are zero except the two nodes where current  $i$ is injected. The value of these currents is, respectively,  $+i$ and  $-i$ . The voltage distribution for each current injection is determined using nodal analysis,

$$
V = L^{-1}E,\t\t(3)
$$

where  $L$  is a grounded Laplacian matrix. The current within each edge is determined by multiplying the voltage matrix V by the weighted directed incidence matrix B of subgraph  $\Gamma_n^s$ ,

$$
I = BV = BL^{-1}E.
$$
 (4)

The total current carried by an edge is the sum of the absolute value of the current for each pair of terminals. The node current is the sum of the total current in the adjacent edges. Thus, those nodes adjacent to the edges carrying large current exhibit a large node current.

The boundary of subgraph  $\Gamma_n^s$  is defined as C, a set of nodes in  $\Gamma_n$  adjacent but not belonging to  $\Gamma_n^s$ . The nodes in C adjacent to the nodes in  $\Gamma_n^s$  with the highest current are added to the subgraph along with the corresponding edges. This process is iteratively repeated until the area limit  $A_{max}$ is reached. Therefore, regions with high current are reinforced whereas those areas with smaller current are left unchanged, maximizing the reduction in resistance per unit of added metal. To illustrate this process, an example seed subgraph is shown in Fig. 8b. Brighter nodes correspond to nodes with high current, whereas the darker nodes represent nodes with small current. In the next iteration, brighter zones are reinforced, leading to a reduction in the impedance in that region (see Fig. 8c). Further iterations reinforce the brightest zones, increasing the conductance until the target area is reached (see Fig. 8d).

Algorithm 3 Evaluate the current metric for each node in subgraph  $\Gamma_n^s$  and set of terminals  $\Theta_n \in \Gamma_n^s$ .

	1: <b>procedure</b> NODECURRENT( $\Gamma_n^s$ , $\Theta$ )
2:	$N= \Gamma_n^s $
	3: $[\Theta]^2 = {\theta' \subseteq \Theta   \theta'  = 2}$
	4: $N_{pairs} \leftarrow  [\Theta]^2 $
5:	$L \leftarrow$ Laplacian matrix of $\Gamma_n^s$
6:	$E \in \mathbb{R}^{(N-1) \times N_{pairs}}$
7:	for each pair $(s, t)$ in $[\Theta]^2$ , $i = 1, 2, \ldots, N_{pairs}$
8:	$E_{s,i} \leftarrow 1$
9:	$E_{t,i} \leftarrow -1$
10:	$V \leftarrow L^{-1}E$
11:	$I\in\mathbb{R}^N$
12:	for $p \in \Gamma_n^s$
13:	$I_p \leftarrow \sum_{i=1}^{N_{pairs}} \sum_{j \in N(\Gamma_n^s, i)} g_p j  V_i - V_j $
14:	return /

**Algorithm 4** Given available space graph  $\Gamma_n$ , seed subgraph  $\Gamma_n^s$ , and set of terminals  $\Theta \in \Gamma_n^s$ , add k nodes from  $\Gamma_n$  to  $\Gamma_n^s$ to reduce the impedance of the subgraph.

	1: <b>procedure</b> SMARTGROW( $\Gamma_n, \Gamma_n^s, \Theta, k$ )
2:	$V_r^c \leftarrow V_n \setminus V_r^s$
3:	$[\Theta]^2 = \{ \theta' \subseteq \Theta \mid  \theta'  = 2 \}$
	4: $N_{pairs} \leftarrow  [\Theta]^2 $
	5: $I \leftarrow \text{NODECURRENT}(\Gamma_n^s, \Theta)$
	6: $I^c \in \mathbb{R}^{ V_n^c }$
	7: for $p \in V_n^c$
8:	$I_p^c \leftarrow \sum_{j \in N(\Gamma_n, p), j \in \Gamma_n^s} I_j$
9:	<b>for</b> $i = 1, 2, , k$
10:	$m \leftarrow \{c \mid I_c = max(I)\}\$
11:	$V_n^s \leftarrow V_n^s \cup m$
12:	$I \leftarrow I \setminus m$
13:	$\Gamma_n^s \leftarrow G_n[V_n^s]$
14:	return $\Gamma_n^s$

## *E. Refinement stage*

Due to the area constraint, the growth process cannot continue indefinitely. Further lowering of the subgraph impedance is however possible without increasing the area using the SmartRefine procedure described in algorithm 5. The areas with the largest and smallest current are identified using the node current metric described in the previous section. Those nodes conducting the smallest current are removed without exhibiting a significant effect on the impedance. Using the vacated metal, those regions carrying large current are reinforced, further reducing the subgraph impedance. This process is illustrated in Figs. 8d to 8f. The nodes behind the terminals in Fig. 8d carry smaller current than the rest of the subgraph. These nodes are removed and replaced by the nodes near the blockages with greater node current.

The SmartRefine process can be viewed as moving nodes from quiescent zones to hot spots. The number of nodes removed per iteration is a design variable. Removing additional nodes each iteration would initially converge faster. At later stages of the refinement process, however, the subgraph is close to being locally optimal; excessive movement would possibly increase the impedance. Moving fewer nodes at later stages of the refinement process would therefore yield a lower impedance.

**Algorithm 5** Given available space graph  $\Gamma_n$ , subgraph  $\Gamma_n^s$ , and set of terminals  $\Theta \in \Gamma_n^s$ , replace k nodes in  $\Gamma_n^s$  by k nodes from  $\Gamma_n$  to reduce the impedance of the subgraph.

1: **procedure** SMARTREFINE( $\Gamma_n, \Gamma_n^s, \Theta, k$ ) 2:  $I \leftarrow \text{NODECURRENT}(\Gamma_n^s, \Theta)$ 3: **for**  $i = 1, 2, ..., k$ 4:  $m \leftarrow \{c \mid I_c = min(I)\}\$ 5:  $V_n^s \leftarrow V_n^s \setminus m$ 6:  $I \leftarrow I \setminus m$ 7:  $\Gamma_n^s \leftarrow \text{SMARTGROW}(\Gamma_n, \Gamma_n[V_n^s], \Theta, k)$ 8: **return**  $\Gamma_n^s$ 

## *F. Subgraph reheating*

The graph-based power routing problem can be viewed as an optimization problem,

Minimize: 
$$
R(\Gamma_n^s, \Theta_n)
$$
 s.t. :  $A(\Gamma_n) \leq A_{max}$ . (5)

From an optimization perspective, the SmartGrow and SmartRefine procedures are a form of gradient descent. The resistance of the subgraph is the objective function and the node current metric is a proxy metric for the gradient of the objective function. These algorithms are, therefore, a form of local optimization where the result is not guaranteed to be a global minimum. To mitigate this issue, the subgraph reheating technique is presented in this section, inspired by the simulated annealing algorithm [27] where the objective function can temporarily increase to explore the design space.

The reheating process consists of two operations, dilation and erosion, inspired by image processing operations. Initially, the subgraph is dilated beyond the area constraint by adding nodes adjacent to the subgraph. After completing the dilation operation, the erosion process commences. Using the node current metric, those nodes with the smallest current are removed from the subgraph, eliminating any redundant nodes while reinforcing the hot spots. The number of dilation iterations determine the extent to which the search space is explored. Additional iterations would explore a wider space while requiring greater runtime for the subsequent erosion process.

#### *G. Back conversion*

Once the reheating process is complete, the resulting subgraph is converted back into a polygon. Recall that each node within the graph  $\Gamma_n$  is associated with a tile within the available space. The subgraph  $\Gamma_n^s$  therefore corresponds to a polygon comprised of multiple merged tiles. A typical PCB consists of several nets. Thus, it is crucial to remove the routed polygon from the available space of other nets.

#### *H. Algorithm runtime analysis*

The runtime of the algorithm depends upon a multitude of parameters including the number of terminals, grain size, and size of the available physical space. The first stage of the algorithm is the available space. Modern polygon clipping algorithms exhibit linear complexity with the number of vertices [28]. The PCB layout may contain more than many hundred thousands of vertices [29]. An early PCB prototype, however, contains much fewer vertices, due to the fewer polygons and simpler geometry. In the case studies presented in section III, fewer than 10,000 vertices are processed, requiring up to 50 seconds for six power rails.

The complexity of the Dijkstra shortest path algorithm is  $O((|V_n|+|E_n|)log|V_n|)$ , where  $V_n$  and  $E_n$  are sets of, respectively, nodes and edges of  $\Gamma_n$ . Due to the rectangular tiling of the available space, the number of edges is approximately twice larger than the number of vertices, yielding

$$
O((|V_n| + 2|V_n|)log|V_n|) = O(|V_n|log|V_n|). \tag{6}
$$

The complexity can be improved by employing alternative algorithms such as A-star [30], which utilizes the location of the nodes to accelerate the search process. The complexity of the Dijkstra algorithm, however, is smaller than the complexity of subsequent stages, namely SmartGrow and SmartRefine. In the case studies, finding the shortest path between all pairs of nodes requires negligible time. Thus, accelerating the shortest path algorithm yields only a marginal improvement in computational performance.

The SmartGrow and SmartRefine algorithms both require computation of the voltages within the graph. These processes require the node current metric to be iteratively computed, requiring a solution of the matrix equation. This step is the main bottleneck of the algorithm, requiring up to 90% of the total runtime. Using sparse linear equation solvers, the complexity of solving a linear equation is  $O(|V|^q)$  where  $q \in [1.5, 3]$  is the scaling exponent which equals 1.5 in the best case and 3.0 in the worst case [31]. Both SmartGrow and SmartRefine solve a single linear equation per iteration. Thus, the runtime for SmartGrow stage  $T_g$  is

$$
T_g = c_g \sum_{i=0}^{k_g - 1} (|V_n^s| - i\Delta V)^q,
$$
 (7)

where  $k_g$  is the number of growth iterations,  $\Delta V$  is the number of nodes added per iteration, and  $c_g$  is the proportionality coefficient. The number of iterations  $k<sub>g</sub>$  during the growth stage is approximately

$$
k_g \approx \frac{A_{max}}{\Delta A},\tag{8}
$$

where  $A_{max}$  is the area of the resulting polygon, and  $\Delta A$ is the area added to the subgraph during each iteration of SmartGrow. Similarly, the runtime for SmartRefine stage  $T_r$ is

$$
T_r = c_r k_r |V_n^s|^q,\t\t(9)
$$

where  $c_r$  is the proportionality coefficient.

The reheating process exhibits a complexity similar to SmartGrow and SmartRefine. The dilation process requires negligible time as compared to the erosion process which requires the node current metric to be evaluated. The runtime  $T_e$  required to apply erosion to a dilated subgraph is

$$
T_e = c_e \sum_{i=0}^{k_e - 1} \left( c_d |V_n^s| - i\Delta V \right)^q, \tag{10}
$$

where  $c_d|V_n^s|$  is the number of nodes after the dilation process,  $c_e$  is the proportionality coefficient,  $\Delta V$  is the reduction in order of the subgraph per iteration, and  $k_e$  is the number of erosion iterations,

$$
k_e = \left\lceil \frac{|V|_d - |V_n^s|}{\Delta V} \right\rceil. \tag{11}
$$

The back conversion process reconstructs a set of polygons from the resulting subgraph. The polygons corresponding to each node are iteratively merged using the union operation, exhibiting  $O(Nlog(N))$  complexity for N vertices. In the worst case, the number of vertices grows linearly with each converted node, yielding a worst case complexity

 $O(|V_n^s|(|V_n^s|-1)) = O(|V_n^s|^2)$ . Practically, however, the union of multiple tiles often yields the same number of vertices. For example, the union of tiles A and B, shown in Fig. 6, has the same number of vertices as tile B. The complexity of the back conversion process is therefore between  $O(|V_n^s|)$  and  $O(|V_n^s|^2)$ .

Greater complexity occurs when the node current metric is evaluated, namely, during the SmartGrow, SmartRefine, and erosion procedures. Combining (7), (9), and (10) yields a complexity of approximately

$$
O\left(\left(\frac{A_{max}}{\Delta A} + k_r + k_e\right)|V_n^s|^q\right). \tag{12}
$$

The number of nodes  $|V_n^s|$  is approximately

$$
|V_n^s| \approx \frac{A_{max}}{\Delta x \Delta y}.\tag{13}
$$

The complexity is

$$
O\Big(\frac{A_{max}}{\Delta A} + k_r + k_e\Big) \Big(\frac{A_{max}}{\Delta x \Delta y}\Big)^q.
$$
 (14)

Therefore, to reduce the computational time, the tile size and incremental increase in area during the growth stage should be increased, while the number of refinement and erosion iterations should be reduced.

## III. VALIDATION OF CASE STUDY

Three practical case studies are presented in this section to demonstrate the validity of the proposed tool. In the first case, as described in subsection III-A, a layout of a portion of the PCB between the PMIC and the two groups of vias is synthesized. In the second case, as described in subsection III-B, the connections among the PMIC, capacitor, and a congested group of vias are established for the six nets. An example of PCB resource planning using SPROUT is described in subsection III-C.

TABLE II COMPARISON OF NORMALIZED IMPEDANCE BETWEEN SPROUT AND MANUAL ROUTING FOR THE TWO RAIL SYSTEM SHOWN IN FIG. 9

	Net	Manual	<b>SPROUT</b>
Normalized inductance	$V_{\bm{D}\bm{D} \bm{1}}$	100	87.5
@ 25 MHz (picohenrys)	Vn de	136	138
Normalized DC	$V_{DD1}$	10.0	10.1
resistance (milliohms)	פת ח	12.7	131

#### *A. Two rail system*

A part of an eight layer PCB for an industrial wireless application is shown in Fig. 9a. The PMIC is placed at the bottom layer and provides power to the two power rails,  $V_{DD1}$ and  $V_{DD2}$ , and the corresponding BGA balls at the top layer. The power rails connect the PMIC inductor to the group of BGA vias on the penultimate (seventh) layer. Dedicated ground planes are placed in layers two, six, and eight.

The manually generated layout is shown in Fig. 9b, and the synthesized layout using SPROUT is shown in Fig. 9c. Note that regular geometries are utilized primarily in the manual layout whereas the automatically generated layout exhibits greater diversity in the shape of the geometries. The



Fig. 9. Automated power routing using SPROUT and manual routing. a) Initial layout with blockage (diagonal hatch), and two rails,  $V_{DD1}$  (dark horizontal hatch) and  $V_{DD2}$  (light vertical hatch). A single PMIC supplies power to the rails using two inductors at bottom layer 8. The inductors are connected to routing layer 7 using a via. Any blockage is shaded with a diagonal pattern. b) Manually routed layout. c) Layout synthesized using SPROUT

impedance of the layouts is extracted using a commercial parasitic extraction tool and compared in Table II. The two layouts (manual and synthesized) exhibit similar impedance characteristics. The difference in resistance does not exceed 3.1%. The inductance of rail  $V_{DD1}$  is reduced by 12% by using SPROUT, whereas the inductance of rail  $V_{DD2}$  is increased by 1.47%.

## *B. Six rail system*

In this case study, SPROUT is applied to a congested BGA arrangement, as shown in Fig. 10a. 612 BGA (306 BGA for six power supply nets and 306 BGA for ground) are located at the top layer, and two PMICs are located in the bottom layer of a ten layer PCB. Each PMIC regulates the current for the three voltage domains. Layers four, six, and eight are used for ground routing, and the power rails are routed on the ninth layer.

The power supply rails are routed and compared to the manual layout. The resulting topologies are shown in Figs. 10b and 10c. Note the visual similarity between the layouts. The DC resistance and loop inductance of each rail are listed in Table III. The loop inductance of the rails generated by SPROUT are 1 to 4% smaller than the manual layout while the difference in DC resistance is below 11%.

The six rail PCB layout is synthesized in approximately 11 minutes using an Intel Core i7-67003.40 GHz eight core computer. Although the manual layout time varies with expertise and software, the typical time for manual layout is significantly greater than the time required by SPROUT. Furthermore, after









Fig. 10. Comparison between the automated power routed layout using SPROUT and manually routed layout. a) BGA placement. The numbers indicate the net of the vias; vias without number are ground vias. b) Layout synthesized using SPROUT and c) manual layout. The routing layer is filled with ground metal shown with diagonal hatch.

setup, SPROUT does not require active human involvement, providing additional reduction in time and labor.

## *C. Area/Impedance Tradeoff*

The quality of the power network can directly influence the performance of an integrated circuit. Noise in power networks produces fluctuations in the load voltage. An excessive reduction in the load voltage increases the delay of the transistors, degrading system performance. Variations in the load voltage are typically mitigated with voltage guard bands [32], [33] or with timing guard bands [34]. Additional voltage produces an unnecessary increase in power consumption [33]. The timing guard directly degrades the performance of the system by reducing the maximum clock frequency. Improving the power network helps reduce voltage fluctuations and, consequently, the power and performance of the system. Additional resources are however required, such as metal and layout area, as well as decoupling capacitors and voltage regulators. A complex tradeoff therefore exists among the system performance, power consumption, and cost.

With the ability to efficiently prototype and evaluate a power network, design tradeoffs can be extensively explored. In this

TABLE IV TARGET AREA OF THE TEST LAYOUTS FOR EXPLORING AREA IMPEDANCE **TRADEOFFS** 

Layout #	Modem	<b>CPU</b>	<b>DSP</b>
	15	15	2.5
2	17.5	17.5	3.125
κ	20	20	3.75
4	22.5	22.5	4.375
5	25	25	5
6	27.5	27.5	$\overline{5.625}$
7	30	30	6.25
Ջ	32.5	32.5	6.875
q	35	35	7.5

case study, the relationship among the area, impedance, and load voltage is investigated in an industrial PCB. Modem, CPU, and DSP power supply nets are routed within a ten layer board containing 86 BGA, as illustrated in Fig. 11a. Two and five decoupling capacitors are placed at the bottom layer of, respectively, the modem and CPU rails. To determine the effects of the additional metal area on the parasitic impedance, nine PCB layout prototypes are generated using SPROUT. The area of the power rails in each prototype is summarized in Table IV. The current demand of each rail is uniformly distributed



Fig. 11. Layout generated using SPROUT for three rails, modem (top left), CPU (center), and DSP module (bottom right), for varying metal area. a) Initial BGA arrangement. The numbers within circles indicate the nets. The vias for ground net are solid black. The hatched rectangles represent the blockages. The size of the vias is intentionally exaggerated to show the nets, b)  $a_{model} = 20.0$ ,  $a_{CPU} = 20.0$ ,  $a_{DSP} = 3.75$ , c)  $a_{model} = 22.5$ ,  $a_{CPU} = 22.5$ ,  $a_{DSP} = 4.38$ , d)  $a_{modem} = 27.5$ ,  $a_{CPU} = 27.5$ ,  $a_{DSP} = 5.62$ , e)  $a_{modem} = 32.5$ ,  $a_{CPU} = 32.5$ ,  $a_{DSP} = 6.88$ , and f)  $a_{modem} = 35.0$ ,  $a_{CPU} = 35.0, a_{DSP} = 7.50$ . Area is normalized.



Fig. 12. Parasitic impedance of PCB rails as a function of area. a) Effective resistance, b) effective inductance, c) minimum load voltage, and d) transistor propagation delay.

within the ball grid array. The modem and CPU are provided with, respectively, two and five decoupling capacitors.

With greater area, the impedance is reduced while increasing the cost of the PCB. To explore this tradeoff, nine layouts with different area for the power rails are generated using SPROUT. Examples of these layouts are shown in Figs. 11b to 11f. Note that with smaller area, the BGA are connected while leaving large voids to satisfy the target area. In contrast, the larger area produces congestion due to a lack of space. The relationship between the area allocated to each rail and the impedance is shown in Figs. 12a and 12b. The resistance of the rails is significantly reduced with additional area. The rate of reduction, however, diminishes with larger area. The inductance of the DSP rail exhibits similar behavior. The inductance of the modem and CPU rails is, however, not significantly reduced due to the decoupling capacitors.

The supply voltage for each rail is 1 volt. The minimum load voltage is shown in Fig. 12c. Despite the greater inductance, the voltage drop in the DSP power rail is significantly less due to the smaller load current. In contrast, the voltage drop in the modem and CPU rails is significantly larger due to the greater load current and current slew rate. Note that the voltage drop in the modem with an area of 27.5 units does not significantly decrease. The blockages likely prevent adding metal to those regions with a high current density, impeding any increase in load voltage. A similar trend is observed in the CPU rail. Beyond 22.5 units, the linear reduction in the voltage drop with area significantly slows, requiring additional metal to produce a similar gain in conductance.

The effect of the reduction in power delivery noise on performance depends upon several factors, such as the quality of the package and PCB power networks and the system and device temperature. The gain in performance can be approximated using guidelines characterizing a specific technology. Guidelines for a 32 nm FinFET technology [35] are used in this case study. The estimated propagation delay is shown in Fig. 12d. Increasing the DSP rail area from 3.75 units to 7.5 units produces a 36 millivolt increase in the minimum voltage. A higher load voltage translates into a 7% reduction in the propagation delay of the transistors. Alternatively, a 36 millivolt reduction in the power supply voltage produces a 7% reduction in dynamic power.

## IV. CONCLUSIONS

The power network design process at the board level is highly influenced by system-level parameters such as the BGA pattern, layer specifications, and placement of the individual components. Changing a floorplan if a target impedance is not satisfied significantly degrades the speed of the development process. To increase the likelihood of satisfying target design objectives, system-level parameters are evaluated to determine appropriate tradeoffs among power, performance, and design time. To accelerate this evaluation process, SPROUT, an automated routing algorithm for power network exploration and prototyping, is introduced here. Based on the node current metric introduced in this paper, a layout of a power network suitable for impedance extraction is automatically synthesized.

The primary contribution of SPROUT is automation of layout prototypes, enhancing exploration of the design space. As compared to manual layouts, automated synthesis requires similar time for PCB prototyping without human involvement, providing significant savings in both time and labor. The impedance of the generated layout is similar to a manual layout, achieving less than a 4% difference in the two case studies. Due to automation, a large number of layout prototypes can be analyzed. By providing greater insight into the layout at early stages of the design process, system parameters can be accurately determined, reducing the likelihood of not satisfying target impedance objectives. The tool is demonstrated on two industrial applications. In addition, area/impedance tradeoffs



Fig. 13. Cross-sectional view of the multilayer routing process. Prohibited areas are filled with a diagonal pattern. a) Available space is determined at each layer. Routing between the source (S) and target (T) is not possible within a single layer. b) Equivalent graph showing potential via locations. c) Via placement. The routing process is decomposed into three single layer routing steps between the local source  $s$  and target  $t$ 

SPROUT is the first board-level automated layout prototyping tool. Further development of the tool is possible using novel techniques, such as neural networks and evolutionary optimization, enabling faster synthesis of power network layouts with superior impedance characteristics.

## APPENDIX

## MULTILAYER ROUTING ALGORITHM

If a routing path between terminals is not possible in a single layer due to the space being disjoint, a routing path can be allocated utilizing vias to connect the different layers. The routing process is decomposed into two parts. The layers through which a routing path are possible are initially determined. Due to the relatively high cost of the vias [36], the number of interlayer connections is also minimized. After placement of the vias, the routing process is decomposed into several single layer routing steps.

To determine the layers connecting the terminals, the routing process, described in Algorithm 6, is utilized. The available space for each layer is determined using Algorithm 1 (see Fig. 13a). The available space within each layer is converted into an equivalent two-dimensional graph. The vertical edges connect the vertices within the adjacent layers through a via. This process produces a three-dimensional graph  $\Gamma_n^{3D}$ , as shown in Fig. 13b. The vertical edges are assigned a higher cost, as compared to those edges within the same layer, to model the higher cost of the via.

Once a three-dimensional graph  $\Gamma_n^{3D}$  is generated, the shortest path between nodes in  $\Theta_n$  is determined using a shortest

**Algorithm 6** Given available space for net *n*,  $A_n =$  $\{A_n^1, A_n^2, ..., A_n^L\}$ , on layers 1 to L, routing terminals  $T_n=$  $\{t_1^{l_1},...,t_k^{l_k}\}$ , and via pitch  $p_{via}$ , determine least expensive multilayer path between terminals.

	1: <b>procedure</b> MULTILAYER $(A_n, T_n, r_{via}, w_{via})$
2:	$\Gamma_n^{3D} = (V_n^{3D} = \emptyset, E_n^{3D} = \emptyset)$
3:	for $l=1,2,,L$
4:	$\Gamma_n^l = (V_n^l, E_n^l) \leftarrow$ SPACETOGRAPH $(A_n^l, \Delta x = \Delta y = r_{via})$
5:	FOR EACH TERMINAL $t_i^{l_i}$ in $T_n$
6:	IF $l_i = l$
7:	$\Gamma_n^l, \Theta_l \leftarrow$ IDENTIFYTERMINALS $(\Gamma_n^l, t_i^{l_i})$
8:	$V_n^{3D} \leftarrow V_n^{3D} \cup V_n^l$
9:	$E_n^{3D} \leftarrow E_n^{3D} \cup E_l^{l}$
10:	FOR EACH VERTEX $v$ IN $\Gamma_n^l$
11:	IF NODE $v^{l-1}$ EXISTS
12:	$E_n^{3D} \leftarrow E_n^{3D} \cup \{v^l, v^{l-1}, w = w_{via}\}\$
	$paths \leftarrow$ SHORTESTPATH $(\Gamma_n, \theta_i, {\{\theta_i+1,\ldots,\theta_k\}})$
13:	FOR $e = \{v_i, v_j\}$ IN paths
14:	$\Theta_i \leftarrow v_i$
15:	$\Theta_i \leftarrow v_i$

16: RETURN  $\Theta = \Theta_1, \Theta_2, ..., \Theta_L$ 

path algorithm, such as Dijkstra [25] or Bellman-Ford [26]. After placing vias, the routing process is separately performed on each layer, from source to via, between vias, and from via to target. Those vias utilized during the routing process between nodes in  $\Theta_n$  become a terminal on the respective layer (see Fig. 13c). The multilayer routing process is thereby split into several two-dimensional routing steps.

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